Name: $\qquad$
Section: $\qquad$
Important: For all three problems, let

$$
A=\left[\begin{array}{ccc}
-1 & 0 & -1 \\
6 & 1 & 8 \\
0 & 0 & 0
\end{array}\right]
$$

1. Find the eigenvalues of $A$ and a basis for each eigenspace.
2. Find a matrix $P$ such that $P^{-1} A P$ is diagonal.
3. Explain in a few words why you could have computed at least one of the eigenvalues of $A$ without using the characteristic polynomial.
